

The Eurasia Proceedings of Science, Technology, Engineering & Mathematics (EPSTEM), 2024

Volume 32, Pages 455-462

IConTES 2024: International Conference on Technology, Engineering and Science

Effect of Porosity on the Nonlinear Thermal Stability of Functionally Graded Material Beams under Various Boundary Conditions

Hichem Bellifa University Djillali Liabes of Sidi Bel Abbes

Abdelmoumen Anis Bousahla University Djillali Liabes of Sidi Bel Abbes

> Abdeldjalil Benbakhti University Centre of Maghnia

Abstract: In this project work, the impact of porosity on the nonlinear thermal buckling response of power law functionally graded beam with various boundary conditions is investigated; the derivation of equations is based on the Euler–Bernoulli beam theory where the distribution of material properties is imitated polynomial function. Using the nonlinear strain–displacement relations, equilibrium equations and stability equations of beam are derived. The beam is assumed under thermal loading, namely: Nonlinear temperature distribution through the thickness. Various types of boundary conditions are assumed for the beam with combination of roller, clamped and simply-supported edges equations for these types of structures. The effects of the porosity parameter, slenderness ratio and power law index on the thermal buckling of P-FG beam are discussed.

Keywords: Euler beam theory, Functionally graded material, Porosity parameter, Thermal buckling

Introduction

During last two decades, the need to design the high per Functionally graded materials (FGMs) are composite materials composed of two or more constituent phases with a continuously variable variation by gradually changing the volume fraction. These materials type have been proposed, developed and successfully employed in industrial application since 1980s (Koizumi, 1993). FGMs were designed as a thermal barrier coating in aerospace application, such as ceramic-metal composite structure.

Nowadays, FGMs are alternative materials widely employed in aerospace, civil, mechanical, nuclear, optical, electronic, chemical, shipbuilding, and biomechanical industries (Akavci, 2016; Kar & Panda, 2015, 2016;Eltaher et al., 2014; Belkorissat et al., 2015; Ait Atmane et al., 2015; Akbas, 2015; Arefi 2015a,2015b;Arefi & Allam, 2015b; Celebi et al., 2016; Darabi & Vosoughi, 2016; Turan et al., 2016; Ebrahimi & Shafiei, 2016; Mouaici al.2016, Mouffoki et al., 2017; Zidi et al., 2017, Bellifa et al., 2017; Karami et al., 2018a, 2019a; Bennai et al., 2019; Bouamoud et al., 2019; Bellifa et al., 2017, 2021; Batou et al., 2019; Chaabane et al., 2019; Alwabli et al., 2021; Benbakhti et al., 2023, 2024; Benfrid et al., 2023; Maachou et al., 2024; Semmah et al., 2024).

The problem of buckling of the porous materials with varying properties has been discussed by many authors. The buckling analysis of thin functionally graded (FG) rectangular plates based on the classical or first order shear deformation theory (FSDT) under various loads were discussed by Mohammadi et al. (2010). Jabbari et al. (2013, 2014) examined porosity distribution influence on buckling characteristics of plates. Buckling of metal foam porous beams using a shear deformation beam model was studied by Chen et al. (2015). In a recent study,

© 2024 Published by ISRES Publishing: <u>www.isres.org</u>

⁻ This is an Open Access article distributed under the terms of the Creative Commons Attribution-Noncommercial 4.0 Unported License, permitting all non-commercial use, distribution, and reproduction in any medium, provided the original work is properly cited.

⁻ Selection and peer-review under responsibility of the Organizing Committee of the Conference

Bellifa et al. (2016) analyzed the wave propagation of an infinite FG plate having porosities by using various simple higher-order shear deformation theories. Ebrahimi et al. (2016) considered the thermal effects on linear free vibration of functionally graded Euler-Bernoulli beams with porosities for pinned-pinned and clamped pinned edges.

To conclude, we have noticed through our reading in the literature that studies on the effect of porosity across the thickness of the FG beam are rare. For this, the aim of this paper first is to extend the Euler–Bernoulli beam theory proposed by Eslami and Kiani (2010) and Bellifa et al. (2017) to porous functionally graded (FG) beams, then to study the critical buckling temperature for FG beams with porosity for different types of boundary conditions and thermal loadings which are assumed to be non-linear distribution through the thickness. Material properties were assumed to be temperature dependent, and graded in the thickness direction according to a simple power law distribution. Finally, the results based on the Euler-Bernoulli beam theory and the effects of thermal loading, porosity, and other parameters on FG beam buckling thermo mechanical behaviour are investigated.

Theoretical Formulations

Kinematics

The classic beam theory is applied throughout the work. Based on the Euler-Bernoulli assumption, the following displacement field can be obtained, (Kiani & Eslami 2010; Belbachir et al., 2024).

$$u(x,z) = u_0(x) - z \frac{\partial w_0}{\partial x}$$

$$v(x,z) = 0$$

$$w(x,z) = w_0(x)$$
(1)

Where $u_0(x, y)$, $w_0(x, y)$ are the two unknown displacement functions of middle surface of the beam in the x and z directions. The Von-Karman-type of geometric non-linearity is taken into consideration in the strain-displacement relations which are as follows

$$\varepsilon_x = \varepsilon_x^0 + z \, k_x \tag{2}$$

Where ε_x^0 and k_x are, respectively, the nonlinear longitudinal strain and curvature defined as (Bellifa and al. 2017)

$$\mathcal{E}_{x}^{0} = \frac{du_{0}}{dx} + \frac{1}{2} \left(\frac{d w_{0}}{dx}\right)^{2} \text{ and } k_{x} = -\frac{d^{2} w_{0}}{dx^{2}}$$
 (3)

Constitutive Relations

Consider a FG rectangular beam with thickness h, length a and width b The Cartesian coordinate system is established so that $0 \le x \le 1$, and $-\frac{h}{2} \le z \le +\frac{h}{2}$.

Functionally graded materials (FGMs) are composed of two kinds of materials: one is a metal and the other is ceramic. Here, Young's modulus E (z) varies continuously through the beams thickness by a polynomial material law. We will consider a non-homogeneity material with a porosity volume function, ξ ($0 \le \xi \le 1$). In such a way, the efficient material properties, as Young's modulus E, the coefficient of thermal expansion α and thermal conductivity K at a point are usually assumed to be given by the rule of mixture (Ait Atmane and al. 2017)

$$E(z) = E_{m} + \left(E_{c} - E_{m}\right) \left(\frac{h+2z}{2h}\right)^{p} - \left(E_{c} + E_{m}\right) \frac{\xi}{2}$$

$$\alpha(z) = \alpha_{m} + \left(\alpha_{c} - \alpha_{m}\right) \left(\frac{h+2z}{2h}\right)^{p} - \left(\alpha_{c} + \alpha_{m}\right) \frac{\xi}{2} \quad (4)$$

$$K(z) = K_{m} + \left(K_{c} - K_{m}\right) \left(\frac{h+2z}{2h}\right)^{p} - \left(K_{c} + K_{m}\right) \frac{\xi}{2} \quad (4)$$

Where p is the volume fraction exponent. The value of p equal to zero represents a fully ceramic beam, whereas infinite p indicates a fully metallic beam. The distribution of the combination of ceramic and metal is linear for p = 1.

The constitutive relation of a FG beam under thermal and mechanical conditions using thermo-elasticity can be expressed as

$$\sigma_x = E(\varepsilon_x - \alpha(T - T_r)) \tag{5}$$

Where σ_x , T and T_r are, respectively, the axial stress, the temperature distribution through the thickness and the reference temperature. The axial force N, the bending moment M caused by thermal stress, respectively are written as

$$(\mathbf{N}, M) = \int_{-\frac{h}{2}}^{\frac{h}{2}} \sigma_x(1, z) dz$$
(6)

By substituting Eq. (4) and Eq. (5) into Eq. (6) we obtain

$$N = \overline{A} \left(\frac{du_0}{dx} + \frac{1}{2} \left(\frac{dw_0}{dx} \right)^2 \right) - \overline{B} \frac{d^2 w_0}{dx^2} - N_T$$

$$M = \overline{B} \left(\frac{du_0}{dx} + \frac{1}{2} \left(\frac{dw_0}{dx} \right)^2 \right) - \overline{C} \frac{d^2 w_0}{dx^2} - M_T$$
(7)

Total potential energy of the FGM beam may be expressed as follows

$$\delta U = \int_{0}^{l} \int_{A} \left(\sigma_x \left(\varepsilon_x - \alpha (T - T_r) \right) \right) dA dx$$
(8)

Substituting Eq.(3) and Eq.(5) into Eq.(8) and integrating with respect to z and y, The total potential energy of the beam is given by

$$\delta U = \frac{b}{2} \begin{bmatrix} \int_{0}^{t} \overline{A} \left(\frac{du_{0}}{dx} + \frac{1}{2} \left(\frac{dw_{0}}{dx} \right)^{2} \right)^{2} - 2\overline{B} \frac{d^{2}w_{0}}{dx^{2}} \left(\frac{du_{0}}{dx} + \frac{1}{2} \left(\frac{dw_{0}}{dx} \right)^{2} \right) \\ + \frac{1}{C} \left(\frac{d^{2}w_{0}}{dx^{2}} \right)^{2} - 2N_{T} \left(\frac{du_{0}}{dx} + \frac{1}{2} \left(\frac{dw_{0}}{dx} \right)^{2} \right) + 2M_{T} \left(\frac{d^{2}w_{0}}{dx^{2}} \right) dx \\ + \int_{0}^{t} \int_{0}^{t} \frac{1}{2} [E(z)\alpha(z)(T - T_{r})] dx \end{bmatrix}$$
(9)

The stability equations of the beam may be derived by the adjacent equilibrium criterion. Assume that the equilibrium state of the FGM beam under thermal loads is defined in terms of the displacement components $(u_0^0, u_0^1, w_0^0, w_0^1)$. The displacement components of a neighboring stable state differ by (u_1, u_2, w_1, w_2) with respect to the equilibrium position. Thus, the total displacements of a neighboring state are

$$u_0 = u_0^0 + u_0^1$$

$$w_0 = w_0^0 + w_0^1$$
(10)

The stability equation of an FGM beam under thermal loading is assumed to be given by eliminating (u_0^1) as

$$\frac{d^4 w_0^1}{dx^4} + \lambda^2 \frac{d^2 w_0^1}{dx^2} = 0$$
(11)

Where

$$\lambda^2 = \frac{AN_T}{\overline{A}\overline{C} - \overline{B}^2}$$
(12)

The parameter λ is a constant and the Eq. (11) is a linear homogeneous equation whose general solution is

$$w_0^1(x) = D_1 \sin(\lambda x) + D_2 \cos(\lambda x) + D_3 x + D_4$$
(13)

Where D_1, D_2, D_3 and D_4 are undetermined constants calculated via the boundary conditions.

$$w_{0}^{1}(x) = D_{1} \sin(\lambda x) + D_{2} \cos(\lambda x) + D_{3}x + D_{4}$$

$$u_{0}^{1}(x) = \frac{\overline{B}}{\overline{A}} \lambda D_{1} \cos(\lambda x) - \frac{\overline{B}}{\overline{A}} \lambda D_{2} \sin(\lambda x) + D_{5}x + D_{6}$$

$$(\overline{A})_{0}^{1}(x) = \frac{\overline{AC} - \overline{B}^{2}}{\overline{A}} \lambda^{2} D_{1} \sin(\lambda x) + \frac{\overline{AC} - \overline{B}^{2}}{\overline{A}} \lambda^{2} D_{2} \cos(\lambda x) + \overline{B} D_{5}$$

$$N_{0}^{1}(x) = \overline{A} D_{5}$$

$$(14)$$

The following boundary conditions are imposed at the edges for FGM beam

$$u_{0}^{1}(0) = w_{0}^{1}(0) = \frac{dw_{0}^{1}}{dx}(0) = u_{0}^{1}(l) = w_{0}^{1}(l) = \frac{dw_{0}^{1}}{dx}(l) = 0$$
⁽¹⁵⁾

Finally, the critical thermal force of the beam, N_{Tcr} for all cases of boundary conditions, can be expressed as follows

$$N_{Tcr} = D \frac{\overline{A}\overline{C} - \overline{B}^2}{\overline{A}(l)^2}$$
(16)

Where D is a constant and depends on the type of boundary conditions (clamped-clamped, simply supported-simply supported, clamped-roller edges, simply supported-roller edges, clamped-simply supported).

Thermal Buckling Solution

Buckling of FGM Beams Under Non-Linear Temperature Across the Thickness

The FGM beams are subjected to transversely non-linear temperature rise, and the increments of temperature on top surface and bottom surface are T_t and T_b , respectively. Four sides of the beam are adiabatic with environment. Due to the increments of transversely temperature inside FGM beams are assumed to be the

function of thickness coordinate z, the increments T = T(z) satisfy the following one-dimensional thermal conduction equation

$$\frac{d}{dz}\left[\left(K(z)\frac{dT}{dz}\right)\right] = 0$$
(17)

This model ignores the time of heat conduction, and the change of temperature due to work produced by the deformations is also neglected. However, the non-linear temperature fields can be obtained easily by using the boundary conditions as

$$T(z) = T_t + \left(\frac{\Delta T}{\Omega}\right) \left[\sum_{i=0}^{5} \frac{(-1)^i}{(ip+1)} \left(\frac{(K_c - K_m)}{K_m}\right)^i \left(\frac{h+2z}{2h}\right)^{(ip+1)}\right]$$
(18)

with

$$\Omega = \sum_{i=0}^{5} \frac{(-1)^{i}}{(ip+1)} \left(\frac{(K_{c} - K_{m})}{K_{m}} \right)^{i}$$
(19)

Numerical Results and Discussion

In this study, various numerical examples are presented and discussed for verifying the accuracy and efficiency of the present theory in predicting buckling stability of FG beams with various boundary conditions under mechanical nonlinear thermal loadings through the thickness. For the verification purpose, the results obtained by the present theory are compared with the existing data in the literature. It is assumed that the functionally graded beam is made of a mixture of aluminum and alumina. The Young modulus and coefficient of thermal expansion for aluminum are $E_m = 70$ GPa, $\alpha_m = 23 \times 10^{-6}$ /°C and $K_m = 204$ W/m°K and for alumina are $E_c = 380$ GPa, $\alpha_c = 7,4 \times 10^{-6}$ /°C and $K_c = 10,4$ W/m°K, respectively. It is assumed that the temperature difference between the metal-rich surface of the FGM and reference temperature is $T_m - T_r = 5^{\circ}C$.

Table 1 present the comparisons of the critical buckling temperature for a CR FG beam under non-linear temperature rise with results of Kiani and Eslami (2015) for different values power law index p. It can be concluded that the results obtained by the present model and those obtained by Kiani and Eslami (2015) are identical for all considered values of power law index p. As we can see, our results are in excellent agreement with those published. It can be concluded that the present theory is efficient for the prediction of critical thermal buckling loads.

Table 1. Critical buckling temperature for a CR FG beam non-linear temperature rise for different values of

power law index p with porosity coefficient	$\xi =$	0,	(l/h=8)
---	---------	----	---------

Temperature load	Theory	р p=0.2	p=1	p=2	p=4	p=5	p=6	p=10
Non linaire	Kiani(2010)	1542.24	965.23	745.45	541.15	325.70	245.12	141.52
	Present	1542.24	965.23	745.45	541.15	325.70	245.12	141.52

Critical buckling temperature of FG beam under linear and non-linear temperature rise for different values of

power law index p, porosity coefficient ξ and thickness ratio l/h is illustrated in table 2. For nonlinear temperature distribution across the thickness, the buckling temperature decreases with the increase of the power law index p. It can be conclude that the critical buckling temperature difference decreases as the thickness ratio and power law index increases and that the maximum critical buckling temperature is obtained with a porosity coefficient equal to $\xi = 0.2$.

			-			-	-					
Ĩ/	$\xi = 0$				ξ = 0.15				$\xi = 0.2$			
h	p=0.2	p=1	p=3	p=8	p=0.2	p=1	<u>p</u> =3	<u>p</u> =8	p=0.2	p=1	<u>p</u> =3	p=8
5	7882.60	5363.8	4153.61	4010.32	9245.12	5843.28	4199.48	605.10	11961.70	6386.96	3764.34	3859.20
3	64	274	44	36	47	16	16	55	43	52	10	09
1	864.933	584.41	451.354	436.378	956.235	637.760	458.349	309.47	1317.658	698.269	409.127	420.814
5	5	05	2	6	7	6	3	40	2	0	2	7
2	303.519	202.05	155.173	150.463	302.452	221.318	159.058	151.27	166 10 15	243.173	140.710	145.743
5	7	72	41	0	1	9	7	63	466.1345	3	1	8
3	148.844	96.714		71 (000)	120.245	106.585	T C CO11	151.27	001 5011	117.789		60 0 5 00
5	5	9	73.5726	71.6903	7	0	/6.6011	63	231.5311	8	66.7585	69.9590
4	85 1021	53.364	20.0070	20 2726	04 2254	50 3604	12 6670	37.819	124 0864	66 1016	36 3257	28 7718
5	83.1921	2	39.9920	39.2730	94.3234	39.3094	42.00/9	1	134.9804	00.1910	30.3237	36.//16

Table 2 Critical buckling temperature for a SS FG beam under non-linear temperature rise for different values of power law index p, porosity coefficient ξ and thickness ratio l/h

Conclusion

This article deals with thermo-mechanical analysis of nonlinear thermal buckling behaviour of porous FG beams with various combinations of boundary conditions under non-linear thermal loadings distribution through the thickness based on Euler–Bernoulli beam theory. Comparison studies are presented out for a large number of beams with different values of thickness ratio, power law index and various combinations of boundary conditions. It can be conclude that the critical buckling temperature difference decreases as the thickness ratio and power law index increases. From the results and the comparisons between the different porosity distributions, it was found that the different distributions give values that are more at least close with the exception of . Finally, some new results critical thermal buckling loads of FG beams with porosity are reported in tabular form for a wide range of thickness ratio and power law index. This new results can be used for comparison with other beam models developed in the future.

Scientific Ethics Declaration

The authors declare that the scientific ethical and legal responsibility of this article published in EPSTEM journal belongs to the authors.

Acknowledgements or Notes

* This article was presented as a poster presentation at the International Conference on Technology, Engineering and Science (<u>www.icontes.net</u>) held in Antalya/Turkey on November 14-17, 2024.

References

- Akavci, S.S. (2016). Mechanical behavior of functionally graded sandwich plates on elastic foundation. *Composites Part B: Engineering*, 96, 136-152.
- Akbas, S. D. (2015). Wave propagation of a functionally graded beam in thermal environments. *Steel and Composite Structures*, 19(6), 1421-1447.
- Alwabli, A., Kaci, A., Bellifa, H., Bousahla A, A., & Tounsi, A. (2021). The nano scale buckling properties of isolated protein microtubules based on modified strain gradient theory and a new single variable trigonometric beam theory. *Advances in Nano Research*, *10*(1) 15-24.
- Arefi, M. (2015a). Elastic solution of a curved beam made of functionally graded materials with different cross sections. *Steel Composite Structures*, 18(3), 659-672.
- Arefi, M. (2015b). Nonlinear electromechanical analysis of a functionally graded square plate integrated with smart layers resting on Winkler-Pasternak foundation. *Smart Structure Systems*, 16(1), 195-211.
- Abdeldjalil, B., Abdelmoutalib, B., Mohamed, C., Rabie, H. Z., & Mohamed, B. B. (2023). Validation of the Ruees-Voight homogenisation model for glass powder-based eco-concretes. *The Eurasia Proceedings* of Science Technology Engineering and Mathematics, 26, 93-99.

- Belbachir, A., Belbachir, N., Bahar, S., Benbakhti, A., Louhibi, Z. S., & Amziane, S. (2024). Unlocking resilience: examining the influence of fluid viscous dampers on seismic performance of reinforcedconcrete structures in earthquake-prone regions. *Periodica Polytechnica Civil Engineering*, 68(4), 1393-1404.
- Bellifa, H., Benrahou, K. H., Hadji, L., Houari, M. S. A., & Tounsi, A. (2016). Bending and free vibration analysis of functionally graded plates using a simple shear deformation theory and the concept the neutral surface position. *Journal of the Brazilian Society of Mechanical Sciences and Engineering*, 38, 265-275.
- Bellifa, H., Tounsi, A., Benbakhti, A., Abdelkader, F., & Benrahou, K. (2017). A new first shear deformation plate theory for dynamic stability analysis of S-FGM plates based on physical neutral surface. In *CFM 2017-23ème Congrès Français de Mécanique*.
- Bellifa, H., Benrahou, K.H., Bousahla, A.A., Tounsi, A., & Mahmoud, S.R. (2017). Nonlocal zerothorder shear deformation theory for nonlinear postbuckling of nanobeams, *Structural Engineering and Mechanics*, 62(6) 695-702.
- Bellifa H., , Bousahla, A., , Chikh, A., Bourada, F., Tounsi, A. (2021). Influence of porosity on thermal buckling behavior of functionally graded beams. *Smart Structures and Systems*, 27(4), 719-728.
- Benbakhti, A., Benfrid, A., Harrat, Z. R., Chatbi, M., Bouiadjra, M. B., & Krour, B. (2024). An analytical analysis of the hydrostatic bending to design a wastewater treatment plant by a new advanced composite material. *Journal of Composite & Advanced Materials/Revue des Composites et des Matériaux Avancés*, 34(2),177-188.
- Benfrid, A., Benbakhti, A., Harrat, Z. R., Chatbi, M., Krour, B., & Bouiadjra, M. B. (2023). Thermomechanical analysis of glass powder based eco-concrete panels: Limitations and performance evaluation. *Periodica Polytechnica Civil Engineering*, 67(4), 1284-1297.
- Chaabane, L. A. (2019). Analytical study of bending and free vibration responses of functionally graded beams resting on elastic foundation. *Structural Engineering and Mechanics, An Int'l Journal*, 71(2), 185-196.
- Chen, D., Yang, J., & Kitipornchai, S. (2015). Elastic buckling and static bending of shear deformable functionally graded porous beam. *Composite Structures*, 133, 54-61.
- Darabi, A., & Vosoughi, A. R. (2016). A hybrid inverse method for small scale parameter estimation of FG nanobeams. *Steel and Composite Structures*, 20(5), 1119-1131.
- Ebrahimi, F., & Barati, M. R. (2016). Thermal buckling analysis of size-dependent FG nanobeams based on the third-order shear deformation beam theory. *Acta Mechanica Solida Sinica*, 29 (5), 547–554.
- Eltaher, M. A., Khairy, A., Sadoun, A. M., & Omar, F. A. (2014). Static and buckling analysis of functionally graded Timoshenko nanobeams. *Applied Mathematics and Computation*, 229, 283-295.
- Feldman, E., & Aboudi, J. (1997). Buckling analysis of functionally graded plates subjected to uniaxial loading. *Composite Structures*, 38(1-4), 29-36.
- Jabbari, M., Mojahedin, A., Khorshidvand, A. R., & Eslami, M. R. (2014). Buckling analysis of a functionally graded thin circular plate made of saturated porous materials. *Journal of Engineering Mechanics*, 140(2), 287-295.
- Jabbari, M., Hashemitaheri, M., Mojahedin, A., & Eslami, M. R. (2014). Thermal buckling analysis of functionally graded thin circular plate made of saturated porous materials. *Journal of Thermal Stresses*, 37(2), 202-220.
- Javaheri, R., & Eslami, M. (2002). Thermal buckling of functionally graded plates. *AIAA Journal*, 40(1), 162-169.
- Karami, B., Shahsavari, D., & Janghorban, M. (2018). Wave propagation analysis in functionally graded (FG) nanoplates under in-plane magnetic field based on nonlocal strain gradient theory and four variable refined plate theory. *Mechanics of Advanced Materials and Structures*, 25(12), 1047-1057.
- Kiani, Y. & Eslami, M. R. (2010). Thermal buckling analysis of functionally graded material beams. *International Journal of Mechanics and Materials in Design*, 6 (3), 229–238.
- Maachou, S., Benbakhti, A., & Moulgada, A. (2024). Comparative study of mechanical behavior between an adhesive made from date palm waste and FM-73 adhesive. In *Materials Science Forum* (Vol. 1125, pp. 65-69). Trans Tech Publications Ltd.
- Najafizadeh, M. M., & Heydari, H. R. (2004). Thermal buckling of functionally graded circular plates based on higher order shear deformation plate theory. *European Journal of Mechanics-A/Solids*, 23(6), 1085-1100.
- Semmah, A., Bellifa, H., Bourada, F., Bousahla, A. A., Tounsi, A., Mohamed, S. M., & Selim, M. M. (2024). Exploring the effect of axial magnetic fields on the thermal stability of SWBNNTs resting on elastic medium using the N-TBT. *The European Physical Journal Plus*, 139(6), 504.
- Simsek, M. (2010). Fundamental frequency analysis of functionally graded beams by using different higherorder beam theories. *Nuclear Engineering and Design*, 240(4), 697-705.

Tounsi, A., Houari, M. S. A., & Benyoucef, S. (2013). A refined trigonometric shear deformation theory for thermoelastic bending of functionally graded sandwich plates. *Aerospace Science and Technology*, 24(1), 209-220.

Author Information						
Hichem Bellifa	Abdelmoumen Anis Bousahla					
University Djillali Liabes of Sidi Bel Abbes, Materials and	University Djillali Liabes of Sidi Bel Abbes, Materials and					
Hydrology laboratory, Algeria	Hydrology laboratory, Algeria					
Contact e-mail: bellifa.hichem@gmail.com						

Abdeldjalil Benbakhti

University Centre of Maghnia, Algeria

To cite this article:

Bellifa, H., Bousahla, A. A., & Benbakhti, A. (2024). Effect of porosity on the nonlinear thermal stability of functionally graded material beams under various boundary conditions. *The Eurasia Proceedings of Science, Technology, Engineering & Mathematics (EPSTEM), 32,* 455-462.